



# **The Case for System Redundancy in Automated Conflict Detection in Aviation: Reducing the False Alert Problem**

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# Examples of Detection/Warning Systems



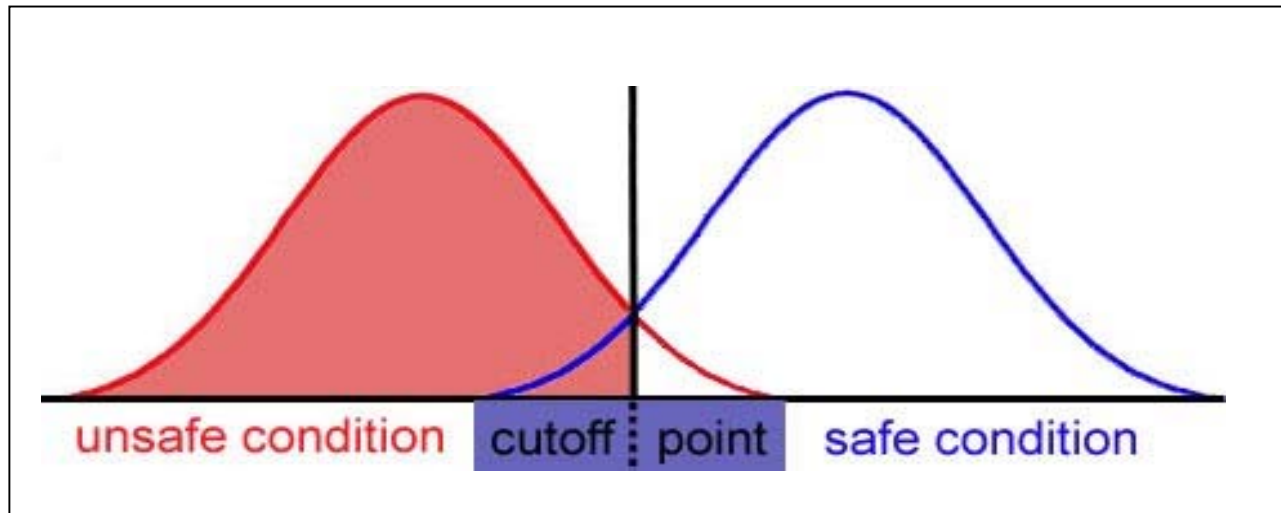
- Smoke Detectors
- Conflict Alerting Systems (FAA Prototype – User Request Evaluation Tool – URET)
- Medical Imaging/Diagnostic Testing
- Baggage Screening



# Attributes of Automated Warning Systems



- Warning systems vary in their ability to discriminate unsafe conditions from safe conditions as a function of the:
  - Effectiveness of the detection algorithms
  - Accuracy/reliability of the input data





# Attributes of Automated Warning Systems (Cont'd)



- Warning systems can be manipulated in terms of the amount of evidence required for an “unsafe” decision
  - Lenient vs. strict alerting threshold
- For a fixed ability to discriminate, increasing the probability of detecting dangerous conditions also increases the probability of false positives.



# Definitions



- $P_d$  – Probability of an alert given an unsafe condition
- $P_{fa}$  – Probability of an alert given a safe condition
- $p$  – Prior odds of an unsafe condition
- $L$  – Likelihood ratio = relative likelihood of an alert in the presence vs. the absence of an unsafe condition =  $P_d \div P_{fa}$
- PPV – Positive predictive value of an alert = a posteriori odds of an unsafe condition given an alert
- Fraction of alerts which are true equals  $PPV \div (1+PPV)$



# Practical Concerns



- Operators may respond slowly or not at all to warnings if the fraction of alerts which are true is too low, possibly below 80 or 90 percent.
- The PPV sufficient to ensure a reliable response is difficult to attain
  - Dangerous situations are usually rare events
  - Problem worsens as you make the alerting threshold more lenient (in order to get a high probability of detecting a dangerous condition; get more false alerts, for a fixed ability to discriminate)



# The Bayesian Approach



- The odds ratio form of Bayes' Theorem:  
**Positive Predictive Value = Prior odds · Likelihood ratio**  
$$PPV = p \cdot L = p \cdot (P_d \div P_{fa})$$
- Some examples:

Prior odds	$P_d$	$P_{fa}$	PPV	Fraction of Alerts Which are True
.001	.99	.05	.0198	2%
.001	.90	.003	0.3	23%
.001	.99	.001	.99	50%
.001	.99	.00011	9*	90%
.0001	.99	.001	.099	9%

\* It is only here that the number of true alerts (warnings indicating a dangerous condition) is greater than the number of false alerts.



# Mitigations



- Choose an optimal alerting threshold based on prior odds and relative costs and benefits of the two kinds of errors; namely, failing to detect a dangerous condition ( $1 - P_d$ ) versus falsely reporting danger ( $P_{fa}$ ). For conflict probe, the threshold may vary depending on the distance between the pair of aircraft.
- Use multiple independent probes
- $L = (P_d^1 \div P_{fa}^1) \cdot (P_d^2 \div P_{fa}^2) \cdot (P_d^3 \div P_{fa}^3) \cdot \dots \cdot (P_d^N \div P_{fa}^N)$  for  $N$  independent probes





## Mitigations (Cont'd)



- For the examples shown in the previous table, adding a single backup probe with  $P_{fa} = .05$  and  $P_d = .99$  would increase PPV by a factor of 19.8.

Prior odds	$P_d$ (First Probe)	$P_{fa}$ (First Probe)	PPV ( $N=2$ Probes)	Fraction of Alerts Which are True
.001	.99	.05	0.39	28%
.001	.90	.003	5.9	86%
.001	.99	.001	19.6	95%
.001	.99	.00011	178	99%
.0001	.99	.001	1.96	66%

- System  $P_d = .99^N$  if each probe has a 99%  $P_d$ .



# First Probe $P_{fa}$ Required for Given PPV



- $P_{fa} = (1/PPV) \cdot P_d^N \cdot p \div (1 - p) \div \text{Backup}_{fa}^N$
- $P_{fa}$  for the first probe scales:
  - Linearly in conflict base rate (since  $p$  is  $\ll 1$ )
  - Inversely with PPV
  - Log-linearly in  $N$
  - Inversely with the  $N$ th power of the backup false alert rate



## Required First Probe $P_{fa}$ (Cont'd)



PPV	Prior odds	$N=1$	$N=2$	$N=3$
9	.001	0.00011	0.0022	0.043
9	.0002	0.000022	0.00044	0.0086
9	.0001	0.000011	0.00022	0.0043

- $N$  is the number of probes
- Each backup probe has a .05 false alert rate
- Each probe has a .99 detection rate: System  $P_d = .99^N$
- PPV = 9: the fraction of alerts which are true = 90%.



# Conclusions



- Developers of automated conflict warning systems should consider the interactions among the
  - Alerting threshold
  - Prior probability of a dangerous condition
  - System sensitivity
- Multiple independent versions of automated conflict probes may be a better strategy than relying on a single version for reducing the false alert problem in automated conflict detection.
- Whether such independent versions can be implemented remains to be determined.
  - Algorithmic diversity does not guarantee independence
  - Common data inputs (e.g., erroneous forecast winds) could cause multiple versions to miss an alert
- Consider partitioning problem: Apply probes separately to portion of problem where they discriminate best.



# References



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